

Colour

Colour

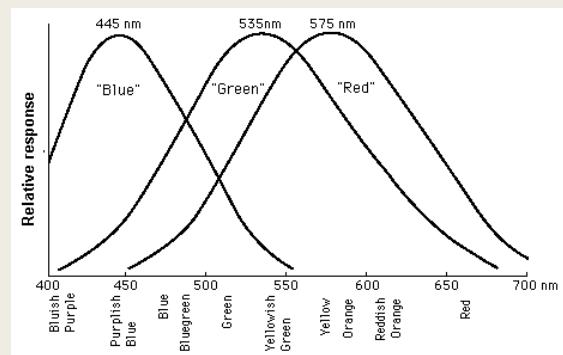
- Look at the meaning of colour – eyes response.
- Colour in the computer.
- Properties of colour. **Hue**, **Saturation** and **Luminance**.
- Limitations of luminance algorithms in computers.
- Colour in Matlab

What is colour?

- Visible light is broken up into wavelengths ranging from Red to Violet. (rainbow)
- This is called the visible spectrum.
- We perceive colours through the stimulation of three types of receptors in our eye called cones.

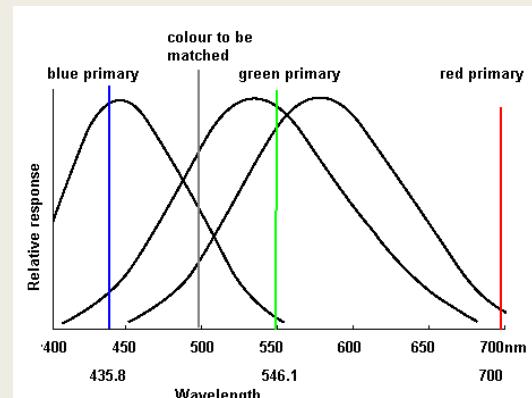
The eye's response to colour

- One cone is more responsive to red, one to green and one to blue.
- But there is overlap.
- Any single wavelength may stimulate more than one type of receptor.



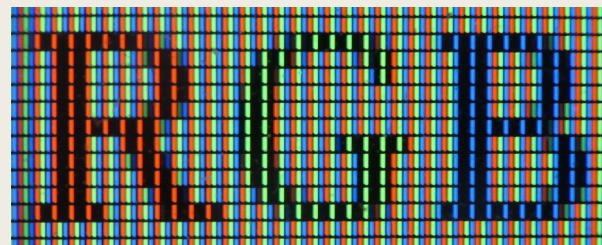
The eye's response to colour

- If we can artificially stimulate the receptors to the same degree as a naturally occurring colour, then the eyes will perceive that colour.
- We therefore try three colours to stimulate the receptors.

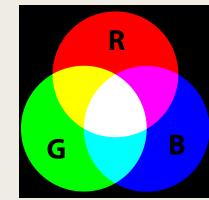


Colour in the computer

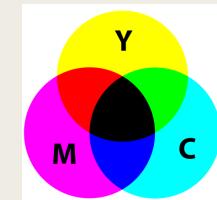
- The computer monitor only emits red, green and blue light.
- It is the combination of these lights which give the perception of colour.
- We fool the eye to “see” other colours.
- However we cannot simulate all colours in this way.



Mixing of colours

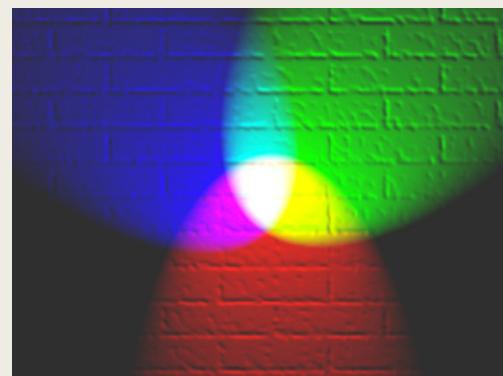


- They are mixed together and the system is arranged so that mixing the maximum (and equal) values of red, green and blue produce a nominal white colour.
- This is called “additive mixing”
- Do not confuse with “subtractive mixing” (dyes) which subtract to give black, this mainly used with printers.



Primary & Secondary colours

- Because **Red**, **Green** and **Blue** are used to produce all the other colours on the computer monitor, they are called **primary colours**.
- If equal amounts of all primary colours give white, what do equal amounts of any two of them give?
 - *Red + Blue gives magenta*
 - *Green + Blue gives cyan*
 - *Red + Green gives yellow*
- These important results are called **secondary colours** and are easily generated.



24 bit colour

- We will consider “true colour” or 24 bit colour in the computer.
- These 24 bits are divided into three groups of 8 bits.
- This gives a range of 0-255 for each colour.
- Each group controls the intensity of the primary colours: red, green and blue.

White or neutral colours

- As mentioned above the maximum equal values of red, green and blue produce white light on the computer monitor.
- That is when red=255, green= 255 and blue=255.
- We can describe this 24 bit colour (in hex) as FFFFFF.
- 3 byte representation



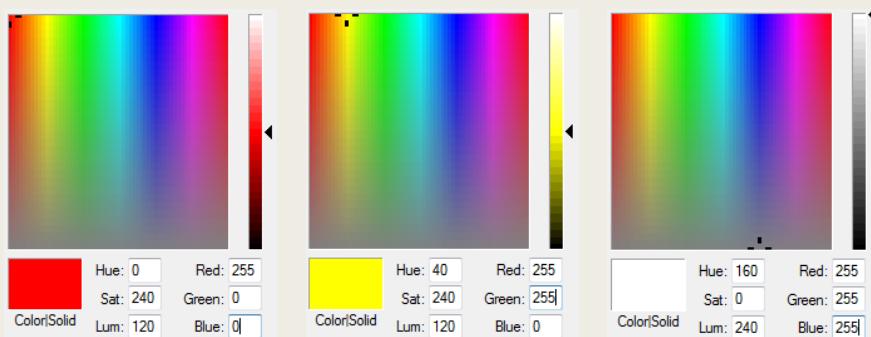
White or neutral colours

- Lesser equal amounts of the three primary colours produce neutral colours (shade of grey).
- Put another way, these combinations have no colour cast.
- Thus the colours:
 - *000000* (0, 0, 0) (*black*),
 - *404040* (64, 64, 64)
 - and *F0F0F0* (240, 240, 240) (*nearly white*)
- are all examples of neutral colours.
- They can be considered as proportions of white.

Gray Shades	HEX	RGB
#000000	rgb(0,0,0)	
#303030	rgb(18,18,18)	
#101010	rgb(16,16,16)	
#181818	rgb(24,24,24)	
#202020	rgb(32,32,32)	
#383838	rgb(40,40,40)	
#303030	rgb(48,48,48)	
#333333	rgb(54,54,54)	
#404040	rgb(64,64,64)	
#484848	rgb(72,72,72)	
#505050	rgb(78,78,78)	
#585858	rgb(88,88,88)	
#606060	rgb(96,96,96)	
#666666	rgb(104,104,104)	
#707070	rgb(112,112,112)	
#777777	rgb(120,120,120)	
#808080	rgb(128,128,128)	
#888888	rgb(136,136,136)	
#909090	rgb(144,144,144)	
#898989	rgb(152,152,152)	
#A0A0A0	rgb(180,180,180)	
#A8A8A8	rgb(188,188,188)	
#B0B0B0	rgb(176,176,176)	
#888888	rgb(184,184,184)	
#C0C0C0	rgb(192,192,192)	
#C8C8C8	rgb(200,200,200)	
#D0D0D0	rgb(208,208,208)	
#D8D8D8	rgb(216,216,216)	
#E0E0E0	rgb(224,224,224)	
#E8E8E8	rgb(232,232,232)	
#F0F0F0	rgb(240,240,240)	
#F8F8F8	rgb(248,248,248)	
#FFFFFF	rgb(255,255,255)	

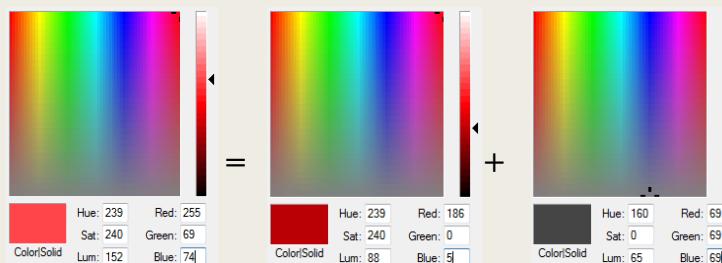
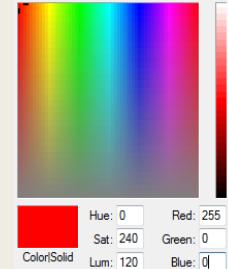
Saturation

- If a colour contains only **one** or **two** primary colours, it is said to be fully (100%) **saturated**.
- In other words the colour is as “strong” (saturated) as it can be. (given the three primary colours).



Saturation

- If we add the missing colour(s) we **desaturate the colour**.
- We are effectively adding some white.
- Take a red colour FF0000 (255,0,0)
- Red and green are missing; so add some.
- FF454A = BA0005 + 454545
- $(255, 69, 74) = (186, 0, 5) + (69, 69, 69)$
- 454545 is the proportion of white we have added.



Saturation

- Adding more white (equal amounts of red, green and blue) desaturates the colour.
- “Pastel” colours are desaturated colours.
- White (and greys) are totally desaturated. (0% saturation)
- For example pink is desaturated red.

Saturation

- From the above description the equation for saturation is intuitive:

$$Saturation = \frac{\max(red, green, blue) - \min(red, green, blue)}{\max(red, green, blue)} \times 100\%$$

- So if any primary colour is missing then $\min=0$ and $\text{saturation}=100\%$
- If all primary colours are present in equal amounts, then $\max=\min$ and $\text{saturation} = 0\%$.

Microsoft Saturation

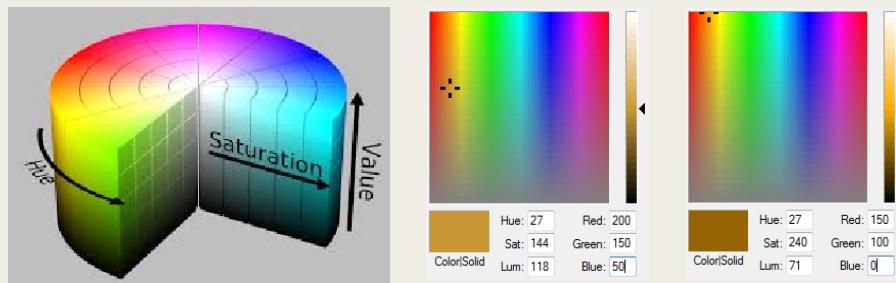
- Microsoft have a different idea about saturation. It is a variation of equation.

$$Saturation = \frac{\max(red, green, blue) - \min(red, green, blue)}{\max(red, green, blue) + \min(red, green, blue)} \times 240$$

- But it is modified according to the brightness values.
- Microsoft set the maximum saturation as 240, that is why we multiply by 240.

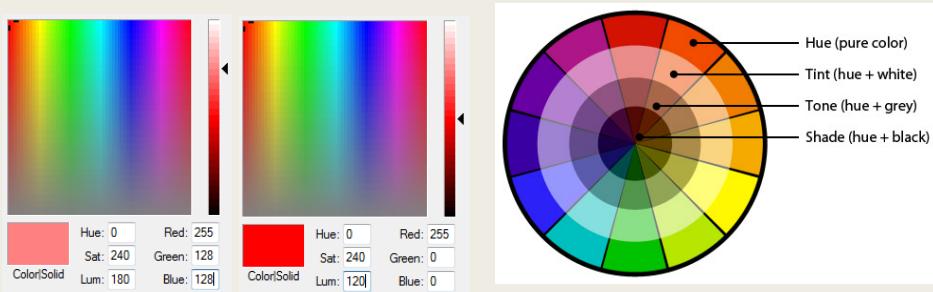
Saturation & Hue

- We can make a desaturated colour saturated by removing the $\min(r,g,b)$ from all colours.
- Then the smallest colour primary will be missing.
- But one property of colour remains the same.
- The colour hue.



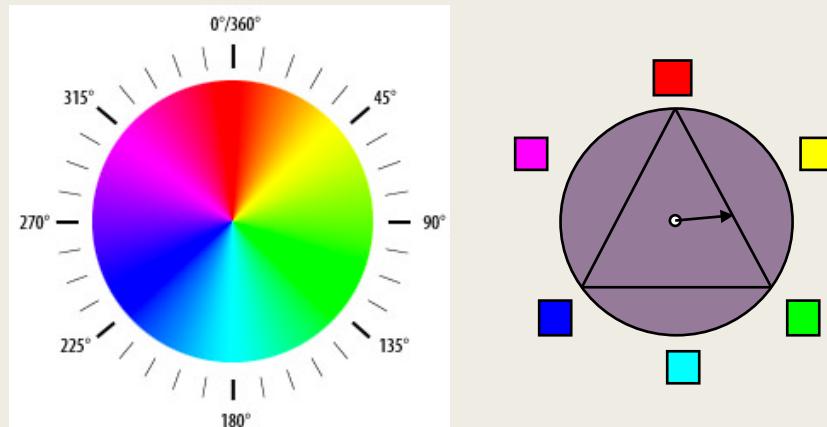
Hue

- Hue is the attribute of a visual sensation according to which an area appears to be similar to one of the perceived colours (e.g., red, green, blue, etc.)
- So pink FF8080 (255,128,128) has the same hue as red.
- It is expressed in degrees around a colour circle.
- Colours from red to blue are arranged around the circle and the colour is specified in degrees.



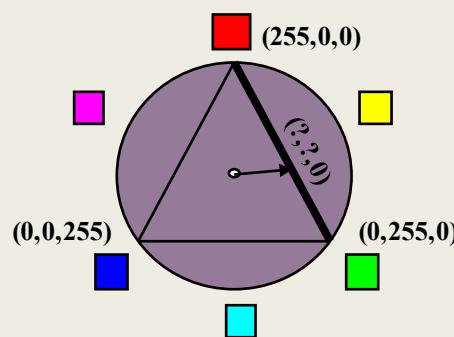
Hue

- Angular position of arrow determines the colour (hue).



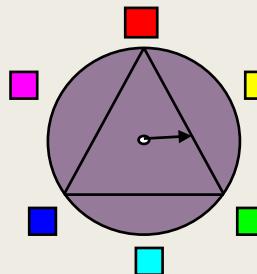
Hue

- Angular position of arrow is determined (and specified) by the distance along the line joining two of the three primary colours.
- All saturated colours lie along these lines.
- We can consider the centre of the circle/triangle as white (totally desaturated).



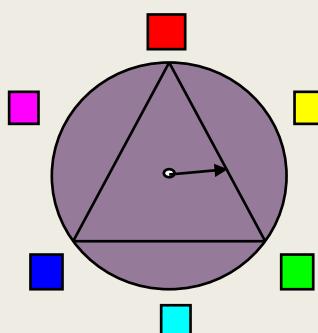
Hue

- **Each of the lines is divided into 120 steps.**
- The beginning and the end of the line correspond to 0, 120, 240 degrees of angle.
- Mid points correspond to 60 degree intervals.
- But the points in between do not (quite).
- Nevertheless they are counted as degrees of colour.
- Easier for computation this way.



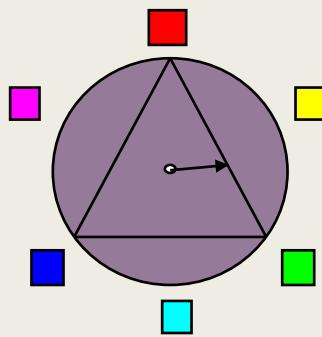
Hue

- So **for saturated colours** , the arrow will lie on one (and only one) of the lines .
 - *If a colour contains only one or two primary colours, it is fully saturated.*
- To **calculate the colour hue** we must find how far along the line the arrow lies.
- For desaturated colours it will point towards one line, unless the colour is neutral



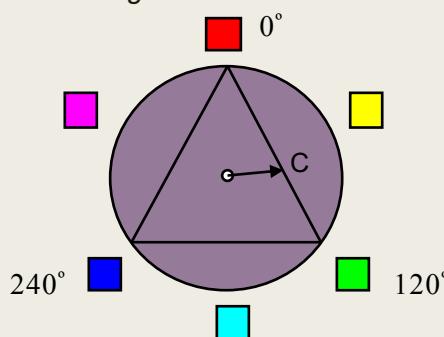
Hue

- In the diagram the arrow lies on the line red to green, but more towards the green primary.
- $\text{Max}(r,g,b)$ will be equal to the green value in this case.
- We have to find how far along the line from red to green it lies.



Hue

- If red corresponds to zero degrees and green corresponds to 120 degrees. How many degrees is point C?
- Well, if green is $\text{max}(r,g,b)$ then:
 - the **point lies between the mid point of the line 60 degrees (red value = green value)**
 - and the green end 120 degrees where the red value=0.



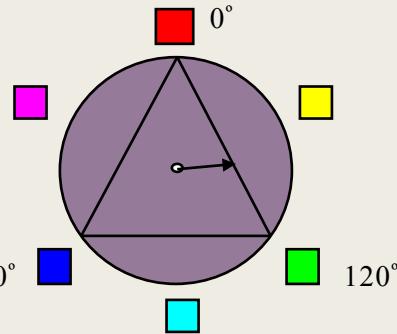
Hue

- An equation to express this would be:

$$\begin{aligned}
 Hue_{\max green} &= 60 \times \left(1 - \frac{\text{red value}}{\text{green value}}\right) + 60 \\
 &= 60 \times \left(2 - \frac{\text{red value}}{\text{green value}}\right)
 \end{aligned}$$

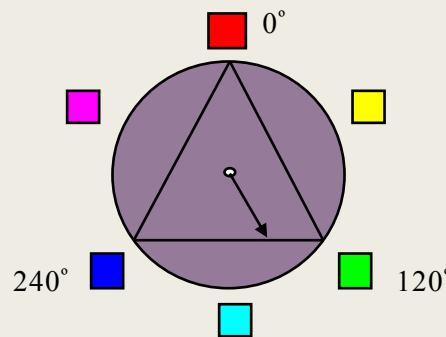
But if green value = max(r, g, b)

$$Hue = 60 \times \left(2 - \frac{\text{red value}}{\max(r, g, b)}\right)$$



Hue

- However, if green is dominant and point C lies on the line between green and blue.
- Then the hue values will vary between green (120 degrees) and the midpoint of the green blue line.



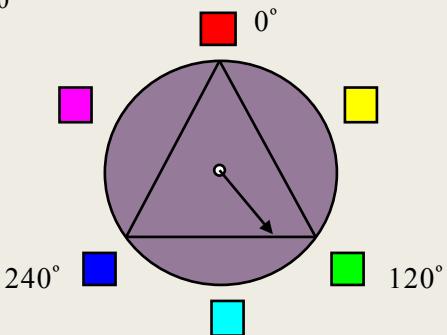
Hue

- An equation to express this would be:

$$\begin{aligned} Hue_{\max green} &= 60 \times \left(1 + \frac{\text{blue value}}{\text{green value}}\right) + 60 \\ &= 60 \times \left(2 + \frac{\text{blue value}}{\text{green value}}\right) \end{aligned}$$

But if green value = $\max(r, g, b)$

$$Hue = 60 \times \left(2 + \frac{\text{blue value}}{\max(r, g, b)}\right)$$



Hue

- We have **not considered unsaturated** colours, when the third colour (red in the second case) is not zero.
- If we subtract the smallest colour (red) from all of the others. The colour will be saturated, but of the same colour hue.
- The resultant arrow will then **lie on one of the adjoining lines** and we can use the equations as before.

$$\begin{aligned} Hue_{\max green} &= 60 \times \left(1 + \frac{\text{blue value}}{\text{green value}}\right) + 60 \\ &= 60 \times \left(2 + \frac{\text{blue value}}{\text{green value}}\right) \end{aligned}$$

But if green value = $\max(r, g, b)$

$$Hue = 60 \times \left(2 + \frac{\text{blue value}}{\max(r, g, b)}\right)$$

Hue

- Subtracting the minimum value (red) in the second case gives

$$Hue = 60 \times \left(2 + \frac{\text{blue value} - \text{red value}}{\max(r, g, b) - \min(r, g, b)} \right)$$

Hue

- And if we do this while considering all primary colours at maximum, we get a set of equations. One for each case.

- When **red** is dominant

$$Hue = 60 \times \left(\frac{\text{green value} - \text{blue value}}{\max(r, g, b) - \min(r, g, b)} \right)$$

- When **green** is dominant

$$Hue = 60 \times \left(2 + \frac{\text{blue value} - \text{red value}}{\max(r, g, b) - \min(r, g, b)} \right)$$

- When **blue** is dominant

$$Hue = 60 \times \left(4 + \frac{\text{red value} - \text{green value}}{\max(r, g, b) - \min(r, g, b)} \right)$$

Hue anomalies

- The first equation **can give negative** values (when red green is minimum. However since the answer is in degrees of a circle **we can add 360 degrees** and get a positive (valid) answer)
- **Microsoft have a values of 240 as maximum hue,**
 - so to convert 360 degrees to 240 Microsoft units we must multiply by:
- $240/360 = 2/3 = 0.667$

Hue

- Lets get the hang of this with some exercises.
- Calculate the colour hue if (in decimal) green=255, blue = 45 and red = 50
 - $\text{Max}(50, 255, 45) = 255$ so **green is dominant** we use

$$Hue = 60 \times \left(2 + \frac{\text{blue value} - \text{red value}}{\max(r, g, b) - \min(r, g, b)} \right)$$

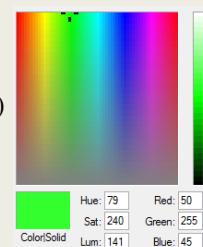
- $\text{Min}(50, 255, 45) = 45$
- So in the equation

$$Hue = 60 \times \left(2 + \frac{\text{blue value} - \text{red value}}{\max(r, g, b) - \min(r, g, b)} \right)$$

$$= 60 \times \left(2 + \frac{45 - 50}{255 - 45} \right)$$

$$= 119^\circ \text{ (rounded)}$$

= 79 Microsoft units. Check it!



Brightness

- Brightness is a perception of the light emitted (or reflected) from an object.
- But our eyes are **more sensitive to green light** than it is for red and blue light.
- For the red, green and blue lights emitted by a computer monitor our eyes sensitivities are **30%, 59%** and **11%** respectively.

Brightness/Value/Intensity/Luma

- Brightness, value, lightness, Intensity are terms used to loosely associate brightness with a colour.
- **HSV** stands for *hue, saturation, and value*. An alternative is **HSB** (*B* for *brightness*)
- In computer systems **no weight is given to the different colours.**
- “Value” is generally taken to be $\max(\text{rgb})$
- Brightness, lightness, “luma” as $(\max(\text{r,g,b}) - \min(\text{r,g,b})) / 2$
 - (*Microsoft, put 240 max, so multiply by 240/255*)
- Intensity as $(\text{r} + \text{g} + \text{b}) / 3$

Hue, Saturation and Brightness

- Find the Hue ,Saturation and Brightness of the following colours.
 - *Red = 240, Green = 100, blue = 50*
 - *Red = 240, Green = 50, blue = 100*
 - *Red = 150, Green = 100, blue = 50*
 - *Red = 40, Green = 100, blue = 150*

Colour spaces

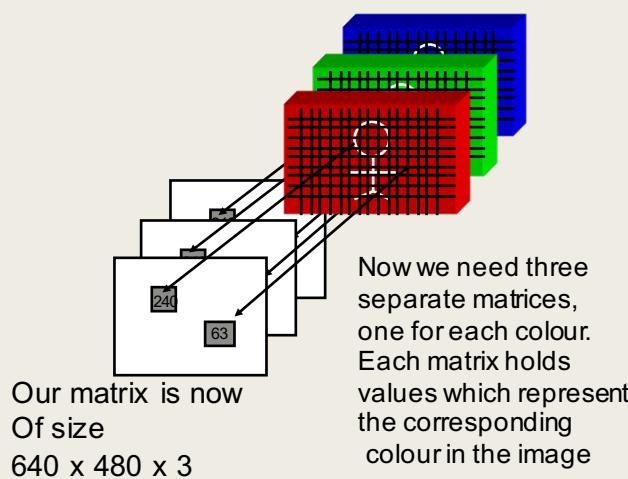
- RGB and HSB are called colour spaces
- This means that a colour can be described by suitable selection of the variables in the colour space.
- Other colour spaces exist
 - *YUV (one luma (Y) and two chrominance (UV) components)*
 - *Lab (L for lightness and a and b for the color-opponent dimensions)*

Production of a greyscale image

- Although a greyscale image can be produced from a colour image, by reducing the saturation in HSL colourspace.
- But better results would be obtained by taking the changes in sensitivity of the eye into account.
- So use from the YUV system

$$Y=0.3R + 0.59G + 0.11B$$

Modifications to our bitmap structure for colour



Colour in Matlab

Exercises

- Matlab stores (as does 24 bit .bmp) colour images in a three dimensional arrays.
- You can think of the array as three colour (two dimensional) pictures/planes, each representing one of the colours red, green and blue, (indexed as 1,2,3 respectively).
- In Matlab syntax

P(row, column, colour) will select a single pixel

So P(40, 50, 2) will select the pixel on row 40, column 50 colour green (2)

Primary colours in Matlab

Exercises

- If we create an 3D array which is filled with zeros to experiment with colour.

mycolarray=zeros(100, 180, 3) ;

Cast it so as to use byte representation:

mycolarray=uint8(mycolarray)

Fill the red plane with 255:

mycolarray(:,:,1)=255

And view it

image(mycolarray)

Primary colours in Matlab

Exercises

- *Reset the red plane to zeros*
 $\text{mycolarray}(:,:,1) = 0$

- *and repeat for green*

$\text{mycolarray}(:,:,2) = 255$

- *and then blue (exercise).*
- *Write a small function to calculate hue, saturation, etc.*
- *Are they as expected?*

White or neutral colours in Matlab

Exercises

- If you fill all the planes with 255 you will get a white image.
- Do this plane by plane as before. (it is possible to do it in one go).
- Change the values in all arrays between 0 and 255.
- The colours should be neutral.
- Save the image

`imwrite(mycolarray, 'myfile.bmp',)`

And inspect using “Paint”

- Look at the hue saturation and brightness values.
- Are they as expected?

Secondary colours in Matlab

Exercises

- You are now going to produce the secondary colours; yellow, cyan and magenta.
- Fill your array with 255 on two of the planes only.
 - Fill blue and green you will get (yellow)
 - Fill red and green you will get (cyan)
 - Fill red and blue you will get (magenta)
- Look at HSL values as before.

The eyes differing sensitivity to colour

Exercises

- Make up an array with the first 60 columns red, the next 60 green and the last 60 blue.
- Use 255 for all values.

```
mycolarray(:,:,:)=0
mycolarray(:,1:60,1)=255
mycolarray(:,61:120,2)=255
mycolarray(:,121:180,3)=255
```

- Look at it.
- What is the brightest colour?
- What is the darkest colour?
- Sketch how you think it would look in monochrome.

The eyes differing sensitivity to colour

Exercises

- Make a monochrome version using the “Microsoft” algorithm, setting red green and blue to equal values giving a neutral image.
 - See *Code 1 at end of presentation*

This would not be a good monochrome picture.

True Luminance

Exercises

- Make a monochrome version using the equation for the Y (Luma) component of YUV.
See Code 2 at end of presentation
- Inspect it
- Now the monochrome image reflects the eyes differing sensitivity to colour.
- Note that all of the band are less than white.
- This allows true white to be represented correctly.

Mix Colours

Exercises

- Create the colours that you used in the Hue exercises.
- Inspect using “Paint”.
- Are the HSL values the same as you calculated.

True luma demo code

Exercises

Code 1

```
mycolarray=double(mycolarray)
mono_msoft(:,:,1) =(max(mycolarray(:,:,3),max(mycolarray(:,:,1), mycolarray(:,:,2)))+ ...
min(mycolarray(:,:,3),min(mycolarray(:,:,1), mycolarray(:,:,2))))/2
mono_msoft(:,:,2) =mono_msoft(:,:,1)
mono_msoft(:,:,3) =mono_msoft(:,:,2)
image(uint8(mono_msoft))
```

Code 2

```
mycolarray=double(mycolarray)
mono_true_lum(:,:,1) =0.3*mycolarray(:,:,1)+0.59*mycolarray(:,:,2)+0.11*mycolarray(:,:,3)
mono_true_lum(:,:,2) = mono_true_lum(:,:,1)
mono_true_lum(:,:,3) = mono_true_lum(:,:,2)
image(uint8(mono_true_lum))
```